

If $f(x)$ is continuous function and $F'(x) = f(x)$ then $\boxed{\int f(x)dx = F(x) + C}$, where C is an arbitrary constant.

Table of basic integrals:

$$1. \int dx = x + C$$

$$2. \int xdx = \frac{x^2}{2} + C$$

$$3. \boxed{\int x^n dx = \frac{x^{n+1}}{n+1} + C} \quad \text{the most widely used...}$$

$$4. \int \frac{1}{x} dx = \ln|x| + C \quad \text{or} \quad \int \frac{dx}{x} = \ln|x| + C$$

$$5. \int a^x dx = \frac{a^x}{\ln a} + C$$

$$6. \int e^x dx = e^x + C$$

$$7. \int \sin x dx = -\cos x + C$$

$$8. \int \cos x dx = \sin x + C$$

$$9. \int \frac{1}{\sin^2 x} dx = -ctgx + C$$

$$10. \int \frac{1}{\cos^2 x} dx = tgx + C$$

$$11. \int \frac{1}{1+x^2} dx = \begin{aligned} & arctgx + C \quad \text{or} \\ & -arcctgx + C \end{aligned}$$

$$\boxed{\int \frac{1}{a^2+x^2} dx = \frac{1}{a} arctg \frac{x}{a} + C}$$

$$12. \int \frac{1}{\sqrt{1-x^2}} dx = \begin{aligned} & \arcsin x + C \quad \text{or} \\ & -arccosx + C \end{aligned}$$

$$\boxed{\int \frac{1}{\sqrt{a^2-x^2}} dx = \arcsin \frac{x}{a} + C}$$

These are the basic tablet integrals. Some professors allow you to use as a tablet:

$$13. \int \frac{dx}{1-x^2} = \frac{1}{2} \ln \left| \frac{1+x}{1-x} \right| + C \quad \boxed{\int \frac{dx}{a^2-x^2} = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right| + C} \quad \text{or} \quad \boxed{\int \frac{dx}{x^2-a^2} = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right| + C}$$

$$14. \int \frac{dx}{\sqrt{x^2 \pm 1}} = \ln \left| x + \sqrt{x^2 \pm 1} \right| + C \quad \boxed{\int \frac{dx}{\sqrt{x^2 \pm a^2}} = \ln \left| x + \sqrt{x^2 \pm a^2} \right| + C}$$